ARL 67-0049 MARCH 1967



## Aerospaco Research Laboratories

# CONDENSATION DROPLET GROWTH IN RAREFIED GASES

SANG-WOOK KANG
CORNELL AERONAUTICAL LABORATORY, INC.
BUFFALO, NEW YORK

Contract No. AF 33(657)-8302 Project No. 7116

Distribution of this document is unlimited



OFFICE OF AEROSPACE RESEARCH United States Air Force



# CONDENSATION DROPLET GROWTH IN RAREFIED GASES

SANG-WOOK KANG

CORNELL AERONAUTICAL LABORATORY, INC. BUFFALO, NEW YORK

MARCH 1967

Contract AF 33(657)-8302 Project 7116

Distribution of this document is unlimited

AEROSPACE RESEARCH LABORATORIES
OFFICE OF AEROSPACE RESEARCH
UNITED STATES AIR FORCE
WRIGHT-PATTERSON AIR FORCE BASE, OHIO

#### **FOREWORD**

This work was sponsored under Air Force Contract AF 33(657)-8302, monitored by Aerospace Research Laboratories, Wright-Patterson Air Force Base, Dayton, Ohio, on Task 711602 of Project 7116, "Research on Hypersonic Condensation Phenomena in High-Temperature Gases".

The author gratefully acknowledges the valuable contributions of Mr. R. C. Weatherston of the Aerodynamic Research Department, Cornell Aeronautical Laboratory, during the course of this work.

#### **ABSTRACT**

高品品

An analysis is made of thermal and diffusion effects on the droplet growth phenomena in a supersaturated vapor and inert carrier gas. Two cases are considered: 1) constant fluid conditions, and 2) changing fluid conditions due to condensation effects. The analysis is so formulated as to describe the continuous growth process as the droplet size increases from microscopic (free-molecular) to "rarefied", even to macroscopic (continuum).

Equations for the conservation of mass and energy are derived by application of the "Langmuir model" in the rarefied ("slip") regime and two correlation parameters for the mass transfer and the energy transfer are introduced for analyzing this regime. Analytic solutions are obtained for the droplet growth with time by expressing the saturation vapor pressure as a linear function of temperature.

The results indicate that the choice of these slip-regime parameters influence the droplet growth only when the ratio of the droplet size to the mean free path is of order one. However, when the droplet size is very small or very large compared to the mean free path, the values chosen for these parameters have a negligible effect on the droplet growth.

# TABLE OF CONTENTS

SECTI	ON	PAGE
1.	INTRODUCTION	1
2.	ANALYSIS FOR CONSTANT FLUID CONDITIONS 2.1 MASS BALANCE 2.2 ENERGY BALANCE	2 2 5
3,	CHANGING FLUID CONDITIONS	9
4.	CONCLUSIONS	FOR CONSTANT FLUID CONDITIONS  SES BALANCE  SERGY BALANCE  SEFLUID CONDITIONS  9  SONS  14
FIGURI		
		16

### LIST OF ILLUSTRATIONS

FIGURE		PAGE
l,A	Model for diffusion analysis—mass transfer	16
lB	Model for analysis—energy transfer	17
2	Energy considerations in the free-molecular regime	18
3	Effect of the variations of slip-regime parameters on droplet growth	19
4	Effect of the variations of energy-transfer parameter on groplet growth with constant mass-transfer parameter	21
5	Effect of the variations of mass-transfer parameter on droplet growth with constant energy-transfer parameter	22
6A	Comparison of the rates of droplet growth for various values of slip-regime parameters	23
6B	Comparison of the rates of droplet growth for various values of energy-transfer parameter with zero mass-transfer parameter	24
6C	Comparison of the rates of droplet growth for various values of mass-transfer parameter with zero energy-transfer parameter	25
7	Effect of the variations of slip-regime parameters on droplet temperature	26
8	Droplet growth under changing fluid conditions for various values of slip-regime parameters	28
9	Droplet growth under changing fluid conditions for various values of slip-regime parameters	29
10	Droplet growth under changing fluid conditions for various droplet concentrations	30
11	Fluid-temperature increase under changing fluid conditions for various droplet concentrations	31
12	Fluid-temperature increase for various values of slip- regime parameters under changing fluid conditions.	32

#### LIST OF SYMBOLS

- A.B Constants defined in Eq (2-10)
- C Vapor concentration (molecules/cm<sup>3</sup>)
- Specific heat at constant pressure (erg/gr-\*K)
- D Droplet diameter (cm)
- $e = 2 \Delta_e$  (cm)
- Heat of condensation, (erg/gr)
- Number of degrees of freedom of a molecule
- ♣ Boltzmann constant = 1.3803 x 10<sup>-16</sup> erg/°K
- K<sub>th</sub> Thermal conductivity of inert gas (erg/cm-sec-°K)
- m Mass of molecule (gr/molecule)
- Partial pressure (dyne/cm<sup>2</sup>)
- Heat flux from a droplet (erg/cm<sup>2</sup>-sec)
- r Radial distance from the center of a droplet (cm)
- Temperature (°K)
- t Time (sec)
- U Internal energy (erg/gr)
- V Flux to a droplet (molecules/cm<sup>2</sup>-sec)
- W Droplet number density (droplets/cm<sup>3</sup>)
- $= 2\Delta_d$  (cm)
- & Sticking coefficient
- y Ratio of specific heats
- A Region I around a droplet (Sec. 2) (cm)
- $\delta_{ik}$  Diffusion coefficient of vapor in inert gas (cm<sup>2</sup>/sec)

- A Mean free path of the gas mixture (cm)
- 5 Slip-regime parameter for energy transfer (Eq(2-28))
- Density (gr/cm<sup>3</sup>)
- or Surface tension (dyne/cm)
- Thermal accommodation coefficient (Eq (2-14))
- Slip-regime parameter for mass transfer (Eq(2-28))

#### SUBSCRIPTS

- c Condensing vapor
- 2 Condensing vapor in 'in 'hase
- D Droplet
- a Inert gas
- r Reflected condition
- sar Saturated equilibrium condition
- d,e Designations of regions of diffusion and of energy transfer, respectively (Fig. 1)
- o Initial condition
- co Condition at large distance from droplet

#### 1. INTRODUCTION

The purpose of the present analysis is to investigate the growth of condensation droplets in rarefied gas when influenced by both thermal and mass-diffusion effects in the supersaturated surrounding fluid. By "rarefied gas" it is meant that the droplet size is of the same order of magnitude as the mean free path of the surrounding gas. As such, the droplet is in the so-called "slip regime". The present study extends an earlier analysis performed by Kang and Weatherston, 1 in which a first-order approximation was employed for the slip regime to investigate the droplet growth from a microscopic size (free-molecular regime) to a macroscopic size (continuum). In that analysis, only a small portion of the total droplet growth process occurred in the slip regime and, consequently, it was not necessary to be too exacting in analyzing that regime. However, if the droplet is in the slip regime, then a more accurate analysis is required. The present analysis deals mainly with the droplet growth in the free-molecular and slip regimes. The analysis, however, is also valid for large final droplet sizes in the continuum regime.

Langmuir<sup>2</sup> pointed out that there is a jump in the vapor concentration at the surface of an evaporating droplet in the transition regime, analogous to the well-known temperature jump at the droplet surface. His observation has led many investigators<sup>3-6</sup> to use the Langmuir model in analyzing either a heat-conduction problem or a mass-transfer process in this regime.

In the present report, the Langmuir model is extended to simultaneously consider both the energy-transfer and mass-transfer processes in the condensation droplet growth under the influence of thermal and diffusion effects. Moreover, in the present analysis, the droplet temperature is left as a variable and is obtained as part of the solution.

In line with the objectives of the present analysis, it is necessary to develop a formulation for droplet growth processes that will apply throughout the free-molecular, slip, and continuum regimes. In both the free-molecular regime, where the mean free path is large compared with the droplet diameter, and the continuum regime, where the droplet is large compared with the mean free path, there are convenient mathematical formulations for analyzing both the mass and energy fluxes. In the slip regime, however, the formulation is not so well established. To bridge the gap between the free-molecular and the continuum regimes, the mass flux at a distance  $\Delta_d$  from the droplet surface is assumed to be the same for the free-molecular or continuum considerations. Similarly, the energy fluxes are matched at a distance  $\Delta_d$ . Thus, a uniform free-molecular field is assumed within the distance  $\Delta$  from the droplet surface, and continuum conditions are assumed to prevail at greater distances (Fig. 1).

The results obtained represent a mathematical fairing between the free-molecular and continuum regimes. In Ref. 1, the free-molecular and continuum effects were equated at the droplet surface proper. This procedure

was known to be somewhat in error, but led to satisfactory results for the purpose of that analysis. Actually, the marked temperature jump within one mean free path of droplet undergoing heat transfer to a fluid would suggest the validity of the Largmuir model, but the mathematical model used here is somewhat of an artifice. However, there is good agreement between experiment and theory if the free-molecular and continuum mechanisms are equated at one mean free path from the droplet surface.

It will be shown that the values assigned to the slip-regime parameters influence the droplet growth only when the ratio of the droplet diameter to the mean free path is near one. When the droplet is very small or very large compared with the mean free path, the values chosen for these parameters have a negligible effect on the droplet growth.

Two situations are considered in the present analysis. In Sec. 2, the growth of a single droplet is studied in a constant fluid medium which consists of an inert carrier gas and the condensing vapor. In Sec. 3, the droplet growth is analyzed for the condition that the surrounding fluid is changing due to condensation, depletion of the mass of vapor in the fluid medium, and release of the heat of condensation to the surroundings.

Closed-form solutions are obtained for the droplet size as a function of time by expressing the saturation vapor pressure as a linear function of temperature. Sample calculations are performed for a nitrogen-mercury gas nuxture under various conditions of pressure and temperature. The initial droplet size is taken to be much smaller than the mean free path of the surrounding gas, so that initially the free-molecular mechanisms will prevail for the droplet growth process. Results are shown to be in general agreement with those obtained in the earlier analysis. I

#### 2. ANALYSIS FOR CONSTANT FIELD CONDITIONS

The formulation of the equations for the solution of the droplet growth and temperature history is similar to that used previously, although the mass and energy transfer in the slip regime is treated somewhat differently in the present analysis.

#### 2.1 MASS BALANCE

It is desired to derive an equation for the mass balance which is applicable not only in the free-molecule and the continuum regimes, but also to the intermediate slip regime. Following Fuchs, the field around a droplet is divided into two regions, as illustrated in Fig. 1. In the immediate vicinity of the droplet (Region Id), between r = D/2 and  $r = \frac{D}{2} + \Delta_d$  (where D is the diameter of the droplet), the free-molecular mechanism is assumed to prevail with the vapor concentration being constant. Outside this region, i.e., in Region II<sub>d</sub>, continuum mechanisms hold. Then, the mass balance yields the following equations.

#### Region Id

It follows, from kinetic theory, 7 that the net number of vapor molecules condensing on the droplet per unit time is:

$$V_{I} = \alpha \pi D^{2} \left( \frac{T_{d}}{\sqrt{2\pi m_{c} A T_{e}}} - \frac{P_{3}}{\sqrt{2\pi m_{c} A T_{3}}} \right) \qquad (2-1)$$

where  $\alpha$  is the sticking coefficient of the vapor and  $p_{\mathbf{p}}$  is the equilibrium pressure on the surface of a droplet with diameter  $\mathbf{p}$  at temperature  $T_{\mathbf{p}}$ . From the physics of small droplets, it is shown that<sup>3</sup>

$$\mathcal{P}_{p} = \mathcal{P}_{\text{ext}}(T_{p}) \exp\left(\frac{4\sigma_{c}m_{c}}{\rho_{c} + T_{p}D}\right)$$
 (2-2)

For a droplet larger than  $5 \times 10^{-6}$  cm in a mercury-nitrogen gas mixture at moderate temperature (of the order of  $500^{\circ}$ K), the exponential term in Eq. (2-2) is very close to unity, and thus  $p_{\rm set}$  can be considered equal to  $p_{\rm set}$ . In addition, the term  $(T_{\rm e}/T_{\rm p})^{1/2}$  is only slightly different from unity, although  $T_{\rm e}-T_{\rm p}$  is not necessarily negligible, as will be shown later in the numerical examples. The error thus introduced into the analysis by setting  $(T_{\rm e}/T_{\rm p})^{1/2}$  equal to unity is negligible. Hence, Eq. (2-1) may be written

$$V_{x} = \frac{\alpha \pi D^{2}}{\sqrt{2\pi m_{c} \pounds T_{p}}} \left( p_{d} - p_{sat} \right)$$
 (2-3)

## Region II<sub>d</sub>

In the continuum, the net number of the vapor molecules passing through  $r=r_a$  per unit time is,  $s=r_a$  using  $(T_a/T_a)^{r_a}\approx 1$ ,

$$V_{\underline{x}} = \frac{2\pi(D + 2\Delta_d)\delta_{12}}{kT_{\underline{x}}} \left(p_{\underline{x}} - p_{\underline{y}}\right) \tag{2-4}$$

Since the net number of the vapor molecules leaving Region II<sub>d</sub> per unit time should all condense on the droplet, we may put  $v_x = v_{\overline{x}}$ . Therefore combining Eqs. (2-3) and (2-4) yields:

$$\mathcal{P}_{d} = \frac{2 \, \delta_{12} \left( D + 2 \, \Delta_{d} \right) \, \mathcal{P}_{\omega} + \alpha \, D^{2} \, \sqrt{\frac{A \, T_{\omega}}{2 \, \pi \, m_{c}}} \, \mathcal{P}_{\text{set}}}{2 \, \delta_{12} \left( D + 2 \, \Delta_{d} \right) + \alpha \, D^{2} \, \sqrt{\frac{A \, T_{\omega}}{2 \, \pi \, m_{c}}}}$$

$$(2-5)$$

<sup>\*</sup>The time required for a droplet to grow from an arbitrarily small size to 5 x 10<sup>-6</sup> cm is infinitesimally small compared with the growth times of interest here, which are of the order of 0.2 to 10 milliseconds.

and introducing  $z = 2\Delta_d$ 

$$V = \frac{\pi D^2 \left(\frac{2\delta_{12}}{kT_{ee}}\right) \left(p_{ee} - p_{est}\right)}{D - \frac{2D}{D+k} + \frac{\delta_{12}}{ee} \sqrt{\frac{8\pi m_c}{kT_{ee}}}}$$
(2-6)

Now, mass balance on a droplet yields

$$\frac{\pi D^2}{m_c} \frac{\rho_c}{2} \frac{dD}{dt} = V \tag{2-7}$$

Substituting Eq. (2-6) and Eq. (2-7) gives

$$\frac{dD}{dt} = \frac{M_1}{D + M_2 - 2 + \frac{Z^2}{D + 2}} (p_a - p_{sat})$$
 (2-8)

where

$$M_{1} = \frac{4 m_{c} \delta_{12}}{\rho_{L} k T_{w}}$$

$$M_{2} = \frac{\delta_{12}}{\alpha} \sqrt{\frac{8 \pi m_{c}}{k T_{w}}}$$
(2-9)

For moderate temperature changes, the saturation vapor pressure of the condensing gas may be assumed to vary linearly with temperature. We may set

$$p_{set}(T_s) = A + B(T_s - T_m)$$
 (2-10)

where A is the saturated vapor pressure at  $T_a$  and B is the proportionality constant which is determined for a specific vapor being considered. Combining Eqs. (2-8) and (c-10) gives:

$$\frac{dD}{dt} = \frac{M_z - M_z \left(T_D - T_\infty\right)}{D + M_z - z + \frac{z^2}{D + z}}$$
 (2-11)

where

$$M_{3} = M_{1} (p_{2} - A)$$

$$M_{4} = M_{1} B$$
(2-12)

#### 2.2 ENERGY BALANCE

As in the mass diffusion case, we wish to obtain an equation for the energy balance between a droplet and its environment which is valid in the rarefied case, as well as in the continuum and free-molecular regimes. In the Langmuir model used here, the environment surrounding a droplet is divided into two regions, as illustrated in Fig. 1B. In Region I, free-molecular mechanism is assumed to prevail; in Region II, exterior to Region I, the continuum mechanism holds.

## Region I<sub>e</sub>

Kinetic theory yields, for the energy balance on a droplet (Fig. 2),

$$\frac{\rho_{e} T_{f}}{2} \frac{dD}{dT} = \frac{\phi_{g} P_{g}}{\sqrt{2\pi m_{g} k T_{e}}} \left(\frac{\dot{f}_{g}^{+} I}{2}\right) k \left(T_{e} - T_{g}\right)$$

$$+ \frac{\left[\alpha + (1 - \alpha) \phi_{c}\right] P_{d}}{\sqrt{2\pi m_{e} k T_{e}}} \left(\frac{\dot{f}_{c}^{+} I}{2}\right) k \left(T_{e} - T_{g}\right) + \alpha \left[\frac{p_{d}}{\sqrt{2\pi m_{e} k T_{g}}} - \frac{p_{g}}{\sqrt{2\pi m_{e} k T_{g}}}\right] \left(\frac{\dot{f}_{c}^{+} I}{2}\right) k T_{g}$$
(2-13)

where the thermal accommodation coefficient is defined as:

$$\phi = \frac{T_r - T_e}{T_p - T_e} \tag{2-14}$$

and T<sub>c</sub> is the temperature corresponding to the energy of a reflected molecule. In Eq. (2-13), the surface-energy term and the term accounting for the droplet-temperature adjustment to the droplet size are not included, due to their negligible effects on the growth process.

By use of Eqs. (2-1) and (2-7), the last term on the right-hand side of Eq. (2-13) may be replaced with

$$\frac{P_{\ell}}{2} \left( U_{\epsilon} + \frac{AT_{9}}{2\pi_{\epsilon}} \right) \frac{dD}{dt}$$

since the internal energy of the vapor per unit mass in gaseous phase is

$$\overline{U}_c = (j_c LT)/(2m_c)$$

Rearranging Eq. (2-13) yields:

$$f_x = M_s \frac{dD}{dt} = (M_b + M_{\gamma})(T_b - T_e)$$
 (2-15)

where

$$M_{s} = \rho_{e} H_{c}/2$$

$$M_{b} = \phi_{g} N_{s}$$

$$M_{T} = \left[ \alpha + (1 - \alpha) \phi_{c} \right] N_{s}$$

$$N_{s} = \frac{k}{2} \left( \frac{r_{g}' + l}{r_{g}' - l} \right) \frac{\rho_{c}}{\sqrt{2\pi m_{g} k T_{co}}}$$

$$(2-16)$$

and

$$N_2 = \frac{k}{2} \left( \frac{r_c + 1}{r_c - 1} \right) \frac{p_\infty}{\sqrt{2 \pi m_c k T_\infty}}$$

### Region II

At  $r_e = \frac{D}{2} + \Delta_e$ , Fourier's equation for continuum heat conduction per unit area of droplet surface gives

$$\mathbf{f}_{\mathbf{z}} = \frac{2 K_{th} \left( T_e - T_e \right)}{\left( \frac{D^2}{D + 2\Delta_e} \right)} \tag{2-17}$$

Now the boundary condition at the juncture of regions  $I_e$  and  $II_e$  requires that  $f_T = f_R$ .

Therefore, combining Eqs. (2-14) and (2-17), we obtain

$$T_{e} = \frac{(M_{6} + M_{7})T_{9} + \frac{2K_{fh}}{D^{2}}(D + 2\Delta_{e})T_{\infty}}{M_{6} + M_{7} + \frac{2K_{fh}}{D^{2}}(D + 2\Delta_{e})}$$
(2-18)

and

$$M_{s} \frac{dD}{dt} = \frac{(M_{6} + M_{7}) 2 K_{th} (D + 2\Delta_{e})}{(M_{6} + M_{7}) D^{2} + 2 K_{th} (D + 2\Delta_{e})} (T_{p} - T_{m})$$
(2-19)

Introducing  $e = 2\Delta_e$  and some manipulation of Eq. (2-19) yields

$$\frac{dD}{dt} = \frac{M_8}{D + M_8 - e + \frac{e^2}{D + e}} \left(T_p - T_{\infty}\right) \tag{2-20}$$

where

$$M_{g} = \frac{4 K_{th}}{P_{L} H_{c}}$$

$$M_{g} = \frac{2 K_{th}}{M_{h} + M_{g}}$$
(2-21)

and  $M_6$ ,  $M_7$  are defined in Eq. (2-16).

Thus, by combining the mass-balance equation (2-11), and the energy-balance equation (2-20), we obtain an expression for the rate of droplet growth.

$$\frac{dD}{dt} = \frac{M_3 M_8 (D+z)(D+e)}{(N_6 D+N_7)(D+z)(D+e) - M_4 \bullet D(D+z) - M_8 \circ D(D+e)}$$
(2-22)

where

$$N_6 = M_4 + M_8$$

$$N_7 = M_2 M_8 + M_4 M_4$$
(2-23)

Integration of Eq. (2-22) with the boundary condition  $D = D_0$  at t = 0, the solution for the droplet size as a function of time is obtained as

$$t = N_3 \left( D^2 - D_0^2 \right) + N_4 \left( D - D_0 \right) + \frac{z^2}{M_3} \ln \left( \frac{D + z}{D_0 + z} \right) + N_5 e^2 \ln \left( \frac{D + e}{D_0 + e} \right)$$
 (2-24)

where

$$N_{3} = \frac{1}{2M_{3}} \left( 1 + \frac{M_{4}}{M_{B}} \right)$$

$$N_{4} = \frac{1}{M_{3}} \left[ M_{2} - 2 + \frac{M_{4}}{M_{B}} \left( M_{q} - e \right) \right]$$

$$N_{5} = \frac{M_{4}}{M_{3} M_{B}}$$
(2-25)

The droplet temperature  $T_3$  as a function of the droplet size is, from Eqs.(2-11) and (2-20)

$$T_{D} - T_{e} = \frac{M_{3}(D + M_{4})(D + z)(D + e) - M_{3}e D(D + z)}{(N_{6}D + N_{7})(D + z)(D + e) - M_{4}e D(D + z) - M_{8}z D(D + e)}$$
(2-26)

For convenience, we introduce the correction parameters  $\psi$  and  $\xi$  in terms of the mean free path  $\lambda$ :

$$z = 2\lambda \Psi$$

$$= 2\lambda \xi$$
(2-27)

or

$$\gamma = \frac{\Delta_d}{\lambda}$$

$$\xi = \frac{\Delta_e}{\lambda}$$
(2-28)

where  $\gamma$  and  $\xi$  are multiplication factors for mass diffusion and energy transfer, respectively.

Fuchs  $^3$  contends that the values of  $\mathcal V$  and  $\xi$  may be between unity and 10. On the other hand, Springer and Tsai<sup>6</sup> take the value of unity and results obtained appear to be in good agreement with experimental data,  $^{10}$ ,  $^{11}$  at least for heat conduction in rarefied gases (see Ref. 6 for comparison). Moreover, Gyarmathy  $^{12}$  suggests taking from 0.5 to unity for these values as deduced from Millikan's oil drop drag experiments.

Numerical examples were calculated for V=1,3,5 and S=1,3,5 at  $T_{\infty}=455^{\circ}\text{K}$ ,  $P_{V}=5$  atm,  $P_{\infty}=0.08$  atm,  $\infty=1$ ,  $P_{\infty}=1$ , and  $P_{\infty}=0.001$  micron. The results are shown in Figs. 3 to 5. It is seen that the droplet growth at a given time t depends greatly upon the values of V and S.

Two observations may be made on the droplet growth from the results. The first is that once the diffusion effect on the droplet growth is taken into account, the heat transfer effect is rather small. This may be seen from Fig. 4, where comparison is made between the growth for  $\psi = \xi = 1$  and that for  $\psi = 1$ ,  $\xi = 5$ . The difference in the growths is very small and, for all practical purposes, may be neglected. On the other hand, we observe in Fig. 5 that increasing the value of  $\psi$  from unity to 5 at a fixed value of  $\xi$  (e.g.  $\xi = 1$ ) causes an appreciable difference in the droplet-size growths. Thus, for the numerical examples calculated, the effects of diffusion are more pronounced than those of energy transfer. This is the same conclusion that was obtained in the previous analysis (Ref. 1) which corresponds to  $\psi = \xi = 0$ .

The second observation is that this limiting case of  $\Psi = \xi = 0$  is usually adequate. The comparison of the curves for  $\Psi = \xi = 1$  and  $\Psi = \xi = 0$  in Fig. 3A reveals that the curves are very close to each other. In other words, if the final droplet is sufficiently large to be in the continuum regime, it makes little difference whether the diffusion and energy-transfer conditions are taken at one mean free path from the droplet ( $\Psi = \xi = 1$ ), or at the droplet surface itself ( $\Psi = \xi = 0$ ). However, if the droplet size is in the slip regime, the relative influence of  $\Psi$  and  $\xi$  on the droplet growth is appreciable, as shown in Fig. 3B, which shows the data of Fig. 3A enlarged and replotted on semi-logarithmic coordinates.

The same conclusion may also be obtained from the consideration of the rate of droplet growth for given  $\gamma$  and  $\xi$  (Eq. (2-22)). For  $\gamma = \xi = 0$ , the growth rate becomes, from Eq. (2-22),

$$\left(\frac{dD}{dt}\right)_{e=\psi=g} = \frac{M_3 M_6}{N_6 D + N_7}$$
 (2-29)

We now compare these two rates by defining

$$\Theta = \frac{dD/dt}{(dD/dt)_{0-\gamma-\epsilon}} - 1 \tag{2-30}$$

Substituting Eqs. (2-22) and (2-29) in Eq. (2-30) gives

$$\Theta = \frac{M_4 e D(D+2) + M_8 z D(D+e)}{(N_6 D+N_7)(D+2)(D+e) - M_4 e D(D+2) - M_8 z D(D+e)}$$
(2-31)

Calculations were performed for the nitrogen-mercury gas mixture under the same conditions as before for various droplet sizes. The mean free path is about 0.02 micron under these circumstances, and the numerical example is calculated for the droplet sizes varying between 0.001 micron and 1.0 micron, which corresponds to the Knudsen number  $\lambda/D$  between 20 and 0.02.

The results are shown in Fig. 6 for various values of  $\mathcal V$  and  $\xi$ . It is seen that there are considerable differences in the rates of the growth, but the resulting droplet sizes, as shown in Fig. 3, are not greatly affected by the particular choice of the parameters  $\mathcal V$  and  $\xi$  as long as the final droplet size is sufficiently large to be in the continuum.

The droplet-temperature history was also obtained for various values of  $\not$  and  $\xi$ , and the results are plotted in Fig. 7. It shows that the droplet temperature jumps about 11 °K from its initial value of  $T_{\omega}$  at the onset of condensation process, decreases slightly and reaches a constant value in a matter of several milliseconds, signifying the balance between the thermal-gradient limitation and the diffusion limitation. This conclusion was also reached in the previous analysis for the case where  $\not$  =  $\xi$  = 0.

#### 3. CHANGING FLUID CONDITIONS

In Sec. 2, the droplet-size growth and the droplet temperature as functions of time were analyzed under thermal and diffusion limitations while the surrounding fluid conditions were assumed to be constant. In this section, the assumption of constant conditions is removed, so that the environmental

conditions such as the fluid temperature and the vapor pressure are allowed to change with time due to the release of the heat of condensation to the surrounding medium as condensation progresses. The changes and the droplet growth now depend upon the droplet number density W, in addition to the other conditions considered in Sec. 2.

In formulating the equations, it is necessary to obtain expressions for the changes in the vapor concentration in the fluid medium  $(p_{\omega})$ , the saturation pressure of the condensing vapor  $(p_{\omega})$ , and the fluid temperature  $T_{\omega}$  in terms of W,  $D_{\omega}$ , and other variables. Of course, the usual mass and energy balances are required. Since these expressions have already been obtained in the previous analysis, their derivations will be omitted here. From Eq. (3-1) of Ref. 1, the fluid temperature  $T_{\omega}$  is

$$T_{or} - T_{o} = G_{e} W \left( D^{3} - D_{o}^{2} \right)$$
 (3-1)

where

$$G_{3} = \frac{\pi k T_{0} \rho_{L} H_{c}}{6 m_{g} c_{\rho_{g}} (p_{r} - p_{0})}$$
(3-2)

The partial vapor pressure of the condensing gas is

$$P_{ab} = C_{16} - G_{7} W D^{3} - G_{8} W^{4} D^{6}$$
 (3-3)

where

$$G_{6} = p_{0} - \frac{p_{0}}{T_{0}} G_{5} W D_{0}^{3} + \frac{w p_{0} k T_{0}}{6 m_{c}} W D_{0}^{3} - \frac{w p_{0} k G_{5}}{6 m_{c}} W D_{0}^{3}$$

$$G_{1} = \frac{m_{R} \& T_{0}}{6m_{c}} - \frac{p_{0}G_{3}}{T_{0}} - \frac{m_{R} \& G_{3}}{3m_{c}} WD_{0}^{3}$$

$$G_{8} = \frac{\pi \rho \, k \, G_{s}}{6 \, m_{c}} \tag{3-4}$$

The saturation pressure of the condensing gas is l

$$p_{set} = (A - BG_s WD^3) + BG_e WD^3 + B(T_p - T_{ac})$$
(3-5)

Combining Eqs. (3-1), (3-3), (3-5), along with the previously developed mass and energy balance Eqs. (2-10) and (2-21), we obtain

$$\left(K_{2}D + K_{1} - K_{4} + \frac{K_{1}}{D + 2} + \frac{K_{4}}{D + e}\right) \frac{dD}{dt} = K_{3} - K_{4}WD^{3} - G_{8}W^{2}D^{4}$$
(3-6)

where

$$K_{1} = \frac{M_{2}}{H_{1}} + BM_{8}M_{4}$$
,  $K_{2} = \frac{1}{M_{1}} + BM_{8}$ ,  $K_{3} = G_{6} - A + BG_{8}WD_{0}^{3}$ ,  $K_{4} = G_{7} + BG_{5}$ ,  $K_{6} = \frac{\pi}{M_{1}} + BM_{8}e$ ,  $K_{7} = \frac{\pi^{2}}{M_{1}}$ ,  $K_{8} = BM_{8}e^{2}$  (3-7)

Integrating Eq. (3-6) by use of integral tables with the boundary condition  $D = D_e$  at t = 0, we obtain

$$t = \frac{1}{6NH^{2}\Omega} \left[ Q_{1}\Omega - Q_{3}H - \frac{H^{3}}{W} (Q_{2}\Omega - Q_{4}H) \right] \left\{ 2n \frac{(H + \Omega D)^{2}}{(H - \Omega D)^{2} + H\Omega D} - 2n \frac{(H + \Omega D)^{2}}{(H - \Omega D_{6})^{2} + H\Omega D_{6}} \right\} + \frac{1}{73NH^{2}\Omega^{2}} \left[ Q_{1}\Omega + Q_{3}H - \frac{H^{3}}{W} (Q_{3}\Omega + Q_{4}H) \right] \times$$

$$\left\{ 2n \frac{(\Omega D/3)}{2H - \Omega D} - 2n \frac{(\Omega D/3)}{2H - \Omega D_{6}} \right\} + \frac{1}{6NF^{2}\Omega^{2}} \left[ Q_{1}\Omega + Q_{3}F + \frac{F^{3}}{W} (Q_{3}\Omega + Q_{4}F) \right] \times$$

$$\left\{ 2n \frac{(F + \Omega D)^{2} - F\Omega D}{(F - \Omega D)^{2}} - 2n \frac{(F + \Omega D)^{2} - F\Omega D}{(F - \Omega D_{6})^{2}} \right\} + \frac{1}{73NF^{2}\Omega^{2}} \left[ Q_{1}\Omega - Q_{3}F + \frac{F^{3}}{W} (Q_{1}\Omega - Q_{4}F) \right] \left\{ 2n \frac{F^{3}}{F + 2\Omega D} - 2n \frac{F^{3}}{F + 2\Omega D} \right\}$$

$$+ \frac{F^{3}}{W} \left( Q_{1}\Omega - Q_{4}F \right) \left\{ 2n \frac{D^{2}}{H^{2}} + K_{8} u_{6} 2n \left( \frac{D + e}{D_{6} + e} \right) \right\}$$

$$+ K_{7}F_{6} 2n \left( \frac{D + e}{D_{7} + 2} \right) + K_{8} u_{6} 2n \left( \frac{D + e}{D_{7} + e} \right)$$

$$- \frac{Q_{6}}{3WK_{4}} 2n \left( \frac{K_{3} - K_{4}WD^{3} - G_{9}W^{2}D^{6}}{K_{3} - K_{4}WD^{3} - G_{9}W^{2}D^{6}} \right)$$

$$+ \frac{(Q_{3} - Q_{4})}{3NW} \left\{ 2n \left( \frac{WD^{3} + H^{3}}{WD^{3} - F^{3}} \right) - 2n \left( \frac{WD_{9}^{3} + H^{3}}{WD^{3} - F^{3}} \right) \right\}$$

$$(3-8)$$

where

$$\Omega = W^{1/3} \qquad N = \sqrt{K_4^2 + 4 K_3 G_8}$$

$$H = \left(\frac{N + K_4}{2 G_8}\right)^{1/3} \qquad F = \left(\frac{N - K_4}{2 G_8}\right)^{1/2} \qquad (3-9)$$

and

$$Q_{1} = K_{1} - K_{6} + K_{7} r_{6} + K_{8} u_{6}$$

$$Q_{2} = K_{7} r_{3} + K_{8} u_{3}$$

$$Q_{3} = K_{4} + K_{7} r_{1} + K_{8} u_{1}$$

$$Q_{4} = K_{7} r_{4} + K_{8} u_{4}$$

$$Q_{5} = K_{1} r_{1} + K_{8} u_{2}$$

$$Q_{6} = \frac{K_{4}}{2G_{8}W} (K_{7} r_{5} + K_{8} u_{5})$$
(3-10)

The terms  $r_o$ ,  $r_i$ ,  $r_s$ , ... and  $u_o$ ,  $u_i$ , ... are defined as

$$\Gamma_{0} = \Gamma_{0} z^{2} W (K_{4} - G_{0} W z^{3})$$

$$\Gamma_{1} = -\Gamma_{0}/z$$

$$\Gamma_{2} = \Gamma_{0}/(z)^{2}$$

$$\Gamma_{3} = \Gamma_{0} W^{2} z^{3} G_{0}$$

$$\Gamma_{4} = -\Gamma_{3}/z$$

$$\Gamma_{5} = \Gamma_{3}/(z)^{3}$$

$$\Gamma_{6} = \frac{1}{K_{4} + W z^{3} (K_{4} - G_{0} W z^{3})}$$
(3-11)

and

$$u_{s} = u_{s}e^{2}W(K_{+}-G_{0}We^{3})$$

$$u_{t} = -u_{o}/e$$

$$u_{2} = u_{o}/(e)^{2}$$

$$u_{3} = u_{6}G_{0}W^{2}e^{2}$$

$$u_{4} = -u_{s}/e$$

$$u_{5} = u_{3}/(e)^{2}$$

$$u_{6} = \frac{1}{K_{3}+We^{3}(K_{4}-G_{0}We^{3})}$$
(3-12)

Thus, an implicit solution is obtained for the droplet size as a function of time in terms of  $\gamma$ ,  $\xi$ ,  $D_o$ , etc.

Numerical examples are calculated under the same initial conditions as in Sec. 2 and the results are plotted in Fig. 8 for W=106 and in Fig. 9 for W=108 with  $\Psi=\xi=0$ , 1, 3, and 5. Fig. 10 gives the droplet growth as a function of time when  $\Psi=\xi=1$  for various values of the droplet number density W. The fluid temperature  $T_{\infty}$  is plotted in Fig. 11 as a function of time for various values of W and  $\Psi=\xi=1$ . Also, the influence of  $\Psi$  and  $\xi$  on the fluid temperature is shown in Fig. 12 where W=107 and  $\Psi$ ,  $\xi$  are varied from 0 to 5.

The results indicate that the effect of  $\mathcal{V}$ ,  $\S$  on the droplet growth is less pronounced in the changing fluid case (Figs. 8, 9) than in the constant fluid case. These figures show that, at a given time t, the droplet-size differences between, say,  $\mathcal{V} = \S = 1$  and  $\mathcal{V} = \S = 5$  become smaller as the magnitude of the droplet number density W is increased. The same trend is also observed for the rate of increase in the fluid temperature as condensation proceeds (Figs. 10, 11). However, in the slip regime itself, the effect of  $\mathcal{V}$  and  $\S$  on the droplet growth is not necessarily small (Fig. 9) and determination of physically reasonable values of  $\mathcal{V}$  and  $\S$  is important in predicting droplet growth in the slip regime. As yet, this

question is not settled to everyone's satisfaction. However, in the case of heat conduction in rarefied gases at least, taking unity for the energy-transfer correlation parameter seems to agree well with the experiment results. 10.11 It appears reasonable to take unit value for the mass transfer parameter as well, since both these processes display similar "jump" characteristics in the slip regime.

#### 4. CONCLUSIONS

The growth characteristics of condensation droplets and the histories of droplet and fluid temperatures in rarefied gases have been analyzed when thermal and diffusion effects are present. Both energy and mass transfer processes are simultaneously considered for the analysis, in which the Langmuir model is employed for the slip regime. Two cases were considered: 1) constant environmental fluid conditions, and 2) the more practical case of the changing fluid conditions due to condensation effects, such as depletion of the mass of the vapor in the fluid medium and the release of the heat of condensation to the surroundings.

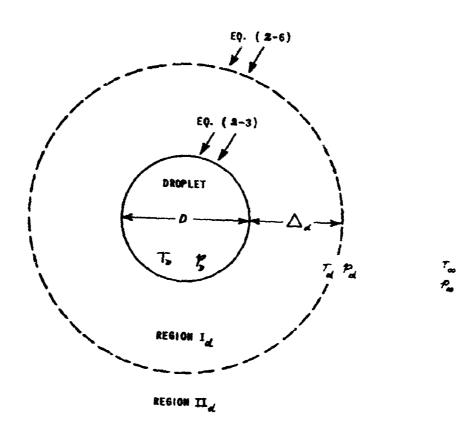
Analytic solutions were obtained for these cases for the droplet size as a function of time by expressing the saturation vapor pressure as a linear function of temperature.

The results indicate that when the droplet is very small or very large compared with the mean free path of the surrounding fluid, the values chosen for the slip-regime parameters  $\mathcal{V}$  and  $\xi$  have a negligible effect on the droplet growth. On the other hand, in the slip regime, the droplet growth depends greatly on the choice of these parameters. Experimental studies are in progress to establish the correct values of those parameters. However, on the basis of limited available heat-transfer data, it appears that taking unit values for these parameters is reasonable.

#### REFERENCES

- 1. Kang, S. and Weatherston, R.C., "An Analysis of Thermal and Diffusion Effects on Droplet Growth Rates." CAL Report AD-1672-A-2 (1966). Also to be published as ARL Report.
- 2. Langmuir, I., J. Amer. Chem. Soc. 37, 426 (1915).
- Fuchs, N.A., Evaporation and Droplet Growth in Gaseous Media.

  Pergamon Press, London (1959).
- 4. Welander, P., Arkiv. F. Fysik. I, 507 (1954).
- 5. Shäfer, K., Rating, K., and Eucken, A., Ann. Physik, 42, 176 (1942).
- 6. Springer, G. and Tsai, S., "Method for Calculating Heat Conduction From Spheres in Rarefied Gases." Phys. Fluids. 8, 1561 (1965).
- 7. Kennard, E., Kinetic Theory of Gases. McGraw-Hill (1938).
- 8. Sherwood, T. and Pigford, R., Absorption and Extraction, 2nd Ed. McGraw-Hill (1952).
- 9. Weber, S., Kgl. Danske Videnskab. Selskab. Mat. Fys. Medd. 19, 11 (1942).
- 10. Takao, P., Memo. of Defense Academy, Yokosuka, Japan, 2, No. 3 (1962).
- 11. Petersen, H., Ph.D. Thesis, Univ. of Missouri (1958).
- 12. Private communication with Dr. G. Gyarmathy, Aerospace Research Laboratories, Wright-Patterson Air Force Base, Ohio



REGION I - FREE-MOLECULAR REGIME REGION II - CONTINUUM REGIME

Figure 14 MODEL FOR DIFFUSION ANALYSIS - MASS TRANSFER

-- 46 %

The second of th

REGION  $\Pi_{\mathbf{a}^+}$  FREE-NOLECULAR REGINE REGION  $\Pi_{\mathbf{a}^+}$  CONTINUUM REGINE

Figure 18 MODEL FOR ANALYSIS - ENERGY TRANSFER

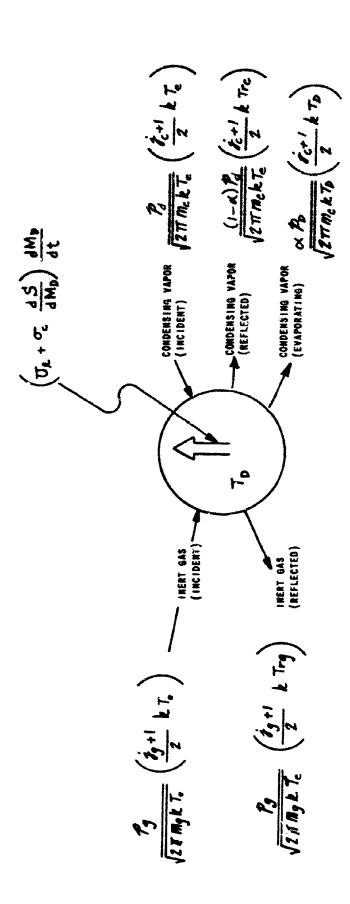


Figure 2 FREEGY CONSIDERATIONS IN THE FREE-MOLECULAR REGIME



THE PERSON NAMED OF THE PERSON NAMED IN COLUMN TWO IS NOT THE PERSON NAMED IN THE PERS

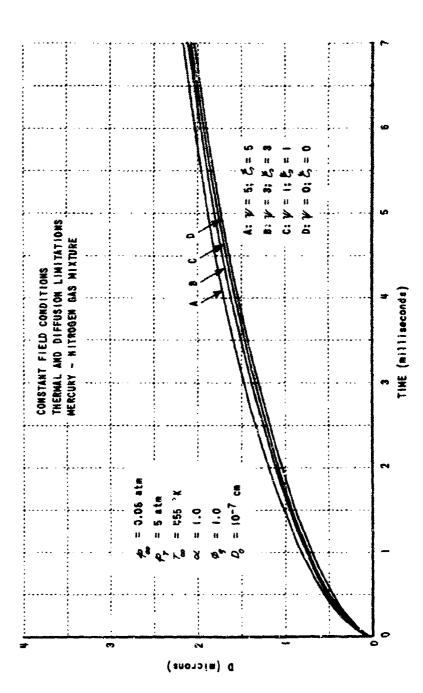
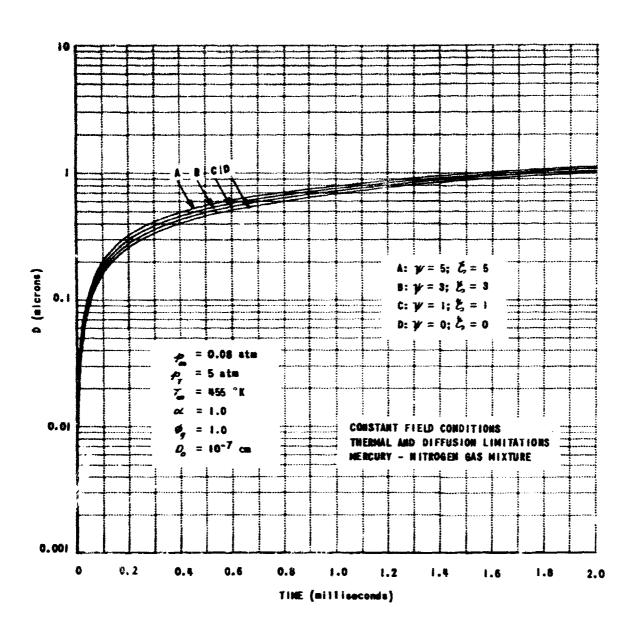
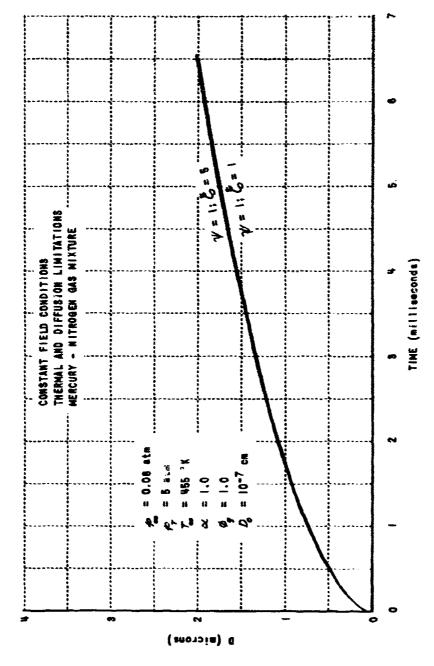


FIGURE 3A EFFECT OF THE VARIATIONS OF SLIP-REGIME PARAMETERS ON DROPLET GROWTH



server over extension and any order over the contract of the c

Figure 38 EFFECT OF THE VARIATIONS OF SLIP-REGIME PARAMETERS ON DROPLET GROWTH



EFFECT OF THE VARIATIONS OF ENERGY-TRANSFER PARAMETER ON DROPLET GROWTH WITH CONSTANT MASS-TRANSFER PARAMETER Figure 4

J. F.

The state of the s

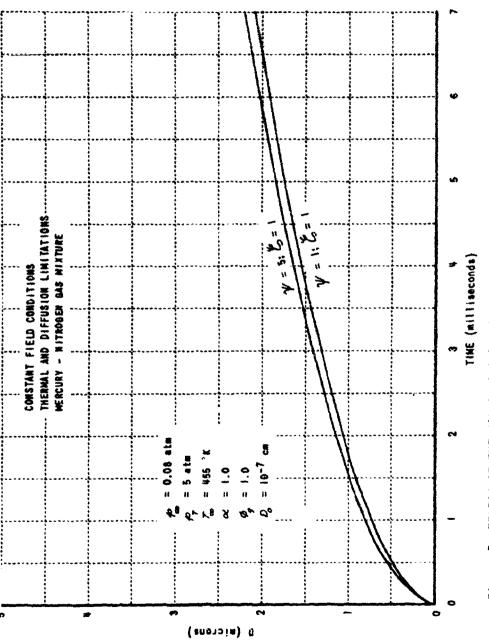
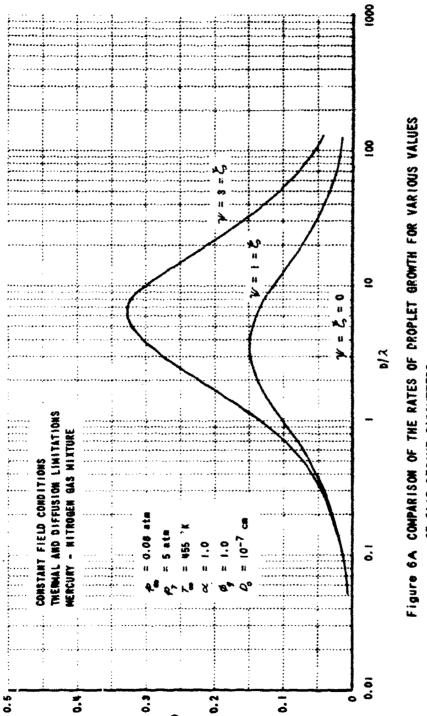
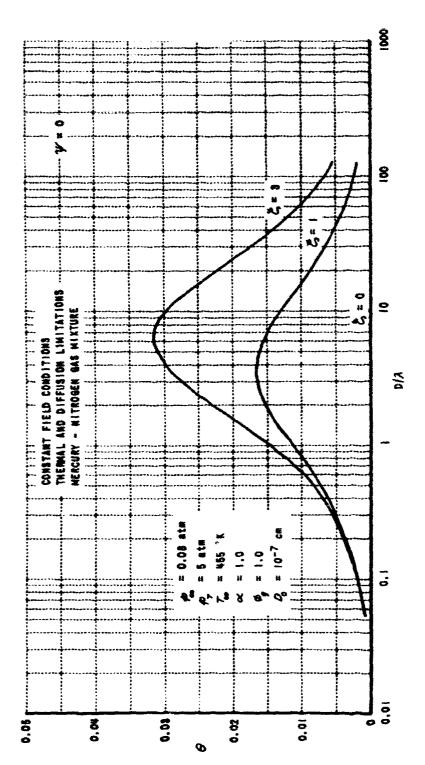


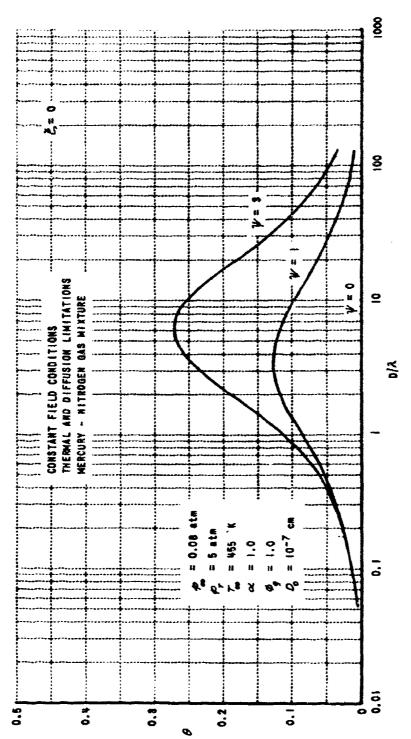
Figure 5 EFFECT OF THE VARIATIONS OF MASS-TRANSFER PARAMETER ON DROPLET GROWTH WITH CONSTANT ENERGY-TRANSFER PARAMETER



OF SLIP-REGIME PARAMETERS



COMPARISON OF THE RATES OF DROPLET GROWTH FOR VARIOUS VALUES OF ENERGY-TRANSFER PARAMETER WITH ZERO MASS-TRANSFER PARAMETER Flgure 63



COMPARISON OF THE RATES OF DROPLET GROWTH FOR VARIOUS VALUES OF MASS-TRANSFER PARAMETER WITH ZERO ENERGY-TRANSFER PARAMETER Figure 6C

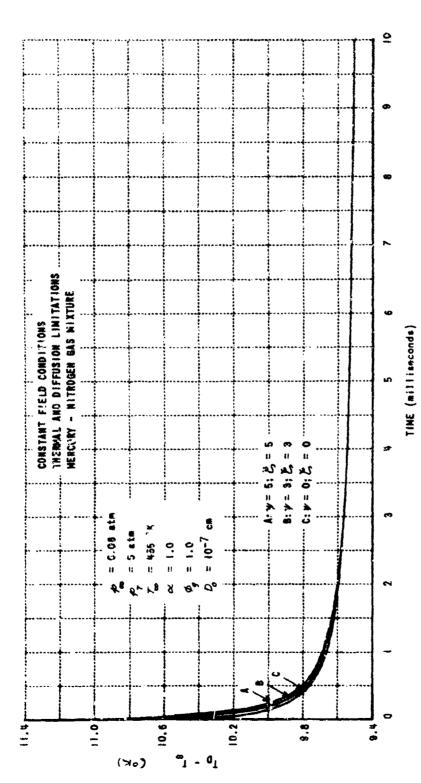


Figure 7A EFFECT OF THE VARIATIONS OF SLIP-REGIME PARAMETERS ON DROPLET TEMPERATURE

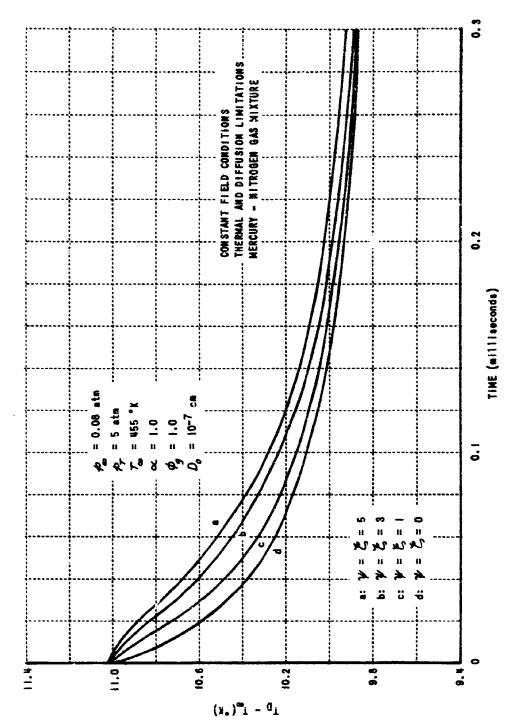


FIGURE 78 EFFECT OF THE VARIATIONS OF SLIP-REGIME PARAMETERS ON DROPLET TEMPERATURE

DROPLET GROWTH UNDER CHANGING FLUID CONDITIONS FOR VARIOUS VALUES OF SLIP-REGIME PARAMETERS Figure 8

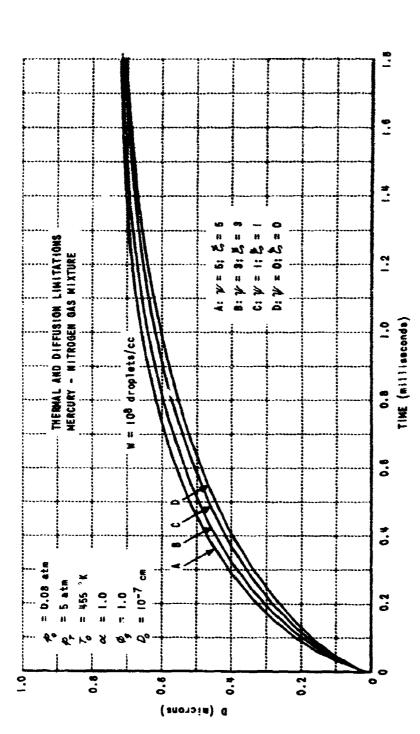


FIGURE 9 DROPLET GROWTH UNDER CHANGING FLUID CONDITIONS FOR VARIOUS VALUES OF SLIP-REGIME PARAMETERS

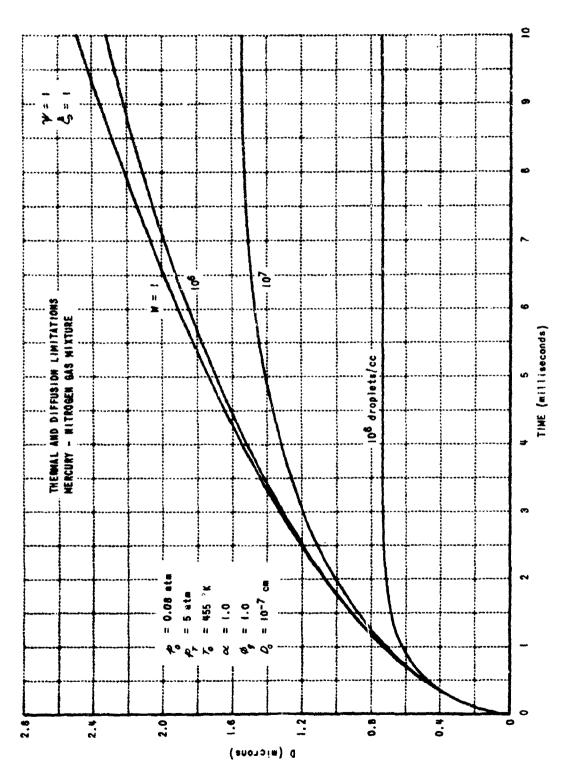


Figure 10 DROPLET GROWTH UNDER CHANGING FLUID CONDITIONS FOR VARIOUS DROPLET CONCENTRATIONS

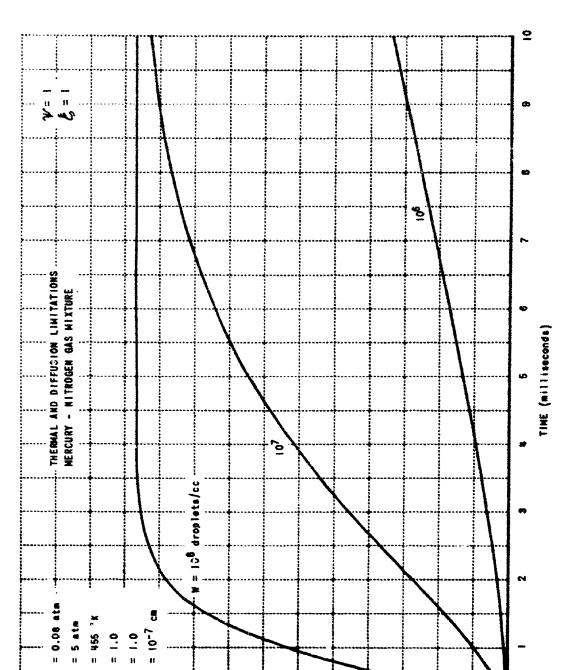


Figure 11 FLUID-TEMPERATURE INCREASE UNDER CHANGING FLUID CONDITIONS FOR VARIOUS DROPLET CONCENTRATIONS

- 19

A CONTRACTOR OF THE PROPERTY O

ەً- ما ت

20

2

24

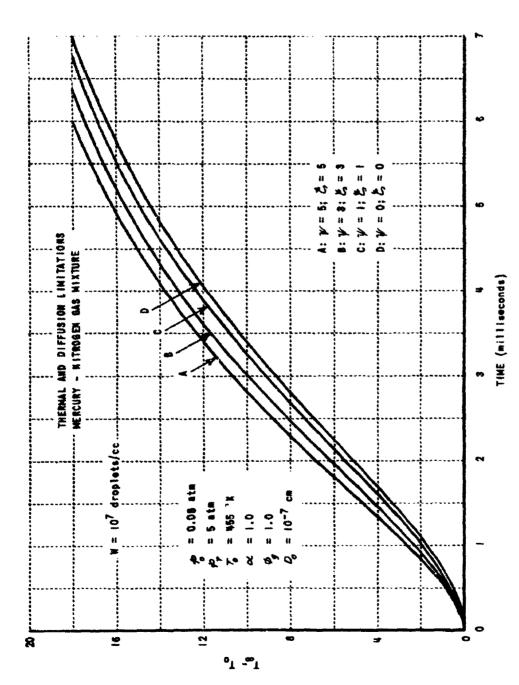


Figure 12 FLUID-TEMPERATURE INCREASE FOR VARIOUS VALUES OF SLIP-REGIME PARAMETERS UNDER CHANGING FLUID CONDITIONS

#### Unclassified

O ECARS SALVOR					
Security Classification		والمراجع والمتعادل والمتعا			
	CUMENT CONTROL DATA - RAD	-			
	struct and indexing emplation must be entered				
1 ORIGINATING ACTIVITY (Casporale author)		Unclassified			
Cornell Aeronautical Labora					
P.O. Box 235	28	25 enous			
Baffalo, New York 14221					
	plet Growth in Rarefied Gas	teg			
4. DESCRIPTIVE NOTES (Type of report and incl					
Scientific. Inter	rim.				
S. AUTHOR(S) (Last name, first name, initial)					
Kang, Sang-Wook					
4. REPORT DATE	7s. TOTAL NO. OF PASES				
March 1967	39	12			
Se CONTRACT OR GRANT NO.	Se. ORIGINATOR'S REPOR	T NUMBER(E)			
AF 33(657)-8302	CAL Day and No	AD 1472 A 2			
<b>в. ряозест но. 7116</b>	CAL Report No	o. AD-1672-A-3			
c. 61445014	36. OTHER REPORT HO(S)	NO(5) (A my other numbers that may be assigned			
± 681308	ARL 67-0049	ARL 67-0049			
10. AVAILABILITY/LIMITATION NOTICES					
l. Distribution of this	document is unlimited.				
11. SUPPLEMENTARY NOTES	12. SPONSORING MILITARY ACTIVITY				
	Aerospace Resea	Aerospace Research Laboratories (ARE)			
•	Wright-Patterson	Air Force Base, Ohio			
lie ememer "An analyzaia ia mad	le of the umal and diffusion s	effects on the deanlet			

sis is made of thermal and diffusion effects on the growth phenomena in a supersaturated vapor and inert carrier gas, Two cases are considered: 1) constant fluid conditions, and 2) changing fluid conditions due to condensation effects. The analysis is so formulated as to describe the continuous growth process as the droplet size increases from microscopic (freemolecular) to "rarefied", even to macroscopic (continuum). Equations for the conservation of mass and energy are derived by application of the "Langmuir model" in the rarefied ("slip") regime and two correlation parameters for the mass transfer and the energy transfer are introduced for analyzing this regime. Analytic solutions are obtained for the droplet growth with time by expressing the saturation vapor pressure as a linear function of temperature. The results indicate that the choice of these slip-regime parameters influence the droplet growth only when the ratio of the droplet size to the mean free path is of order one. However when the droplet size is very small or very large compared to the mean free path. the values chosen for these parameters have a negligible effect on the droplet growth.

DD .5084. 1473

Unclassified
Security Classification

Unclassified

	KEY #OROS	Lit	LINK A		LIMK #		LINK C	
	AET WORDS	ROLE	WY	ROLE	wf	MOLE	WT	
thermal and di	ffusion effects							
droplet growth								
supersaturated							,	
			1					
			1					
				1				
			1					
		1						
			1	<u> </u>		<u> </u>		

- I. ORIGINATING ACTIVITY: Enter the name and address of the contractor, subcontractor, grantee, Department of De-
- fense activity or other organization (corporate author) insuing the report.

  2a. REPORT SECURITY CLASSIFICATION: Enter the over-
- 2a. REPORT SECURITY CLASSIFICATION: Enter the overall security classification of the report. Indicate whether "Restricted Data" is included. Marking is to be in accordance with appropriate security regulations.
- 2b. GROUP: Automatic downgrading is specified in DaD Directive 5200.10 and Armed Forces Industrial Manuel. Enter the group number. Also, when applicable, show that optional markings have been used for Group 3 and Group 4 as authorized.
- 3. REPORT TITLE: Enter the complete report title in all capital letters. Titles in all cases should be unclassified. If a meaningful title carmot be selected without classification, show title classification in all capitals in parenthesis inneediately following the title.
- 4. DESCRIPTIVE NOTES: If appropriate, enter the type of report, e.g., interim, progress, summary, actual, or final. Give the inclusive dates when a specific reporting period is covered.
- 5. AUTHOR(5): Enter the name(s) of suthor(s) as shown en or in the report. Enter last name, first name, middle initial. In unitiary, show rank and branch of service. The name of the principal exthor is an absolute minimum requirement.
- 6. REPORT DATE: Enter the date of the report as day, month, year, or month, year. If more than one date appears on the report, use date of publication.
- 7a. TOTAL NUMBER OF PAGES: The total page count should follow normal pagination procedures, i.e., enter the number of pages containing information.
- 75. NUMBER OF REFERENCES: Enter the total number of references cited in the report.
- 8a. CONTRACT OR GRANT NUMBER: If appropriate, enter the applicable number of the contract or grant under which the report was written.
- 86, 8c, & 8d. PROJECT NUMBER: Enter the appropriate military department identification, such as project number, subproject number, system numbers, tank number, etc.
- 9a. ORIGINATOR'S REPORT NUMBER(S): Enter the official report number by which the document will be identified and controlled by the originating activity. This number must be unique to this report.
- 9b. OTHER REPORT NUMBER(S): If the report has been assigned any other report numbers (either by the originator or by the aponsor), also enter this number(s).
- 10. AVAILABILITY/LIMITATION NOTICES: Enter any limitations on further dissemination of the report, other than those

- imposed by security classification, using standard statements such as:
  - (1) "Qualified requesters may obtain copies of this report from DDC."
  - (2) "Foreign announcement and dissemination of this report by DDC is not authorized."
  - (3) "U. S. Government agencies may obtain copies of this report directly from DDC. Other qualified DDC users shall request through
  - (4) "\*U. 8. military systems may obtain copies of this report directly from DDC. Other qualified users shall request through
  - (5) "Al! distribution of this report is controlled. Qualified DDC users shall request through
- If the report has been furnished to the Office of Technical Services, Department of Commerce, for sale to the public, indicate this fact and enter the price, if known.
- 11. SUPPLEMENTARY NOTES: Use for additional explanatory sotes.
- 12. SPONED: ING MILITARY ACTIVITY: Enter the name of the departmental project office or laboratory aponauring (paying for) the research and development. Include address.
- 13. ABSTRACT: Enter an abstract giving a brief and factual aummery of the document indicative of the report, even though it may also appear eleawhere in the body of the technical report. If additional space is required, a continuation sheet shall be attached.

It is highly desirable that the abstract of classified reports be unclassified. Each paragraph of the abstract shall end with an indication of the military security classification of the information in the paragraph, represented as (TS), (S), (C), or (U)

There is no limitation on the length of the abstract. However, the suggested length is from 150 to 225 words.

14. KEY WORDS: Key words are technically meaningful terms or short phrases that characterize a report and may be used as index entries for cataloging the report. Key words must be selected so that no security classification is required. Identifiers, such as equipment model designation, trade name, military project code name, geographic location, may be used as key words but will be followed by an indication of technical context. The essignment of links, rules, and weights is optional.